

Geometry      The Geometry of the Circle  
 Notes - 13- 8    Tangents and Secants in the Coordinate Plane

(5)

Ex. 1: Find the coordinates of the point at which the line  $y = 2x - 1$  intersects a circle with center  $(0, -1)$  and the radius of length  $\sqrt{20}$

line  $y = 2x - 1$

circle  $x^2 + (y + 1)^2 = 20$

$$(x-h)^2 + (y-k)^2 = r^2$$

$$x^2 + (2x - 1 + 1)^2 = 20$$

$$x^2 + (2x)^2 = 20$$

$$x^2 + 4x^2 = 20$$

$$\frac{5x^2}{5} = \frac{20}{5}$$

$$x^2 = 4$$

$$x = \pm 2$$

→ find y

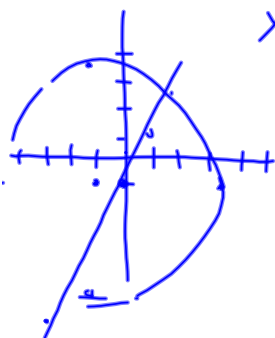
$$x = 2 \quad y = 2(2) - 1 = 3$$

$$x = -2 \quad y = 2(-2) - 1 = -5$$

$(2, 3)$

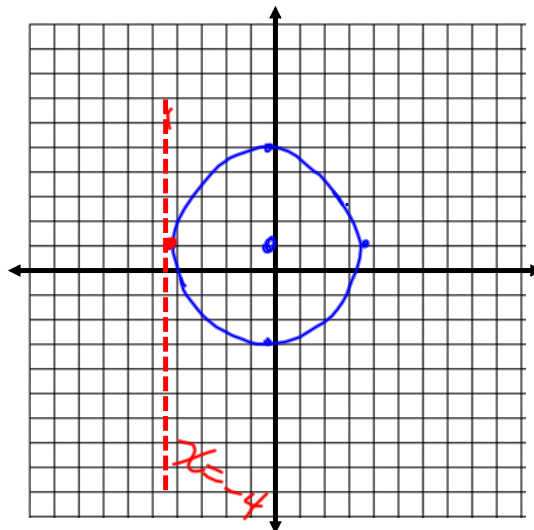
$(-2, -5)$

$$(x-h)^2 + (y-k)^2 = r^2$$



Ex. 2: Write the equation of a line tangent to the circle  $x^2 + y^2 = 16$  at the point  $(-4, 0)$ .

$(0, 0) \quad r = 4$



Ex. 3: Write an equation of the secant that intersects  $x^2 + y^2 = 25$  at A(3,4) and B(0,5).

Slope  $\frac{y_2 - y_1}{x_2 - x_1} = \frac{5 - 4}{0 - 3} = \frac{1}{-3} = -\frac{1}{3}$

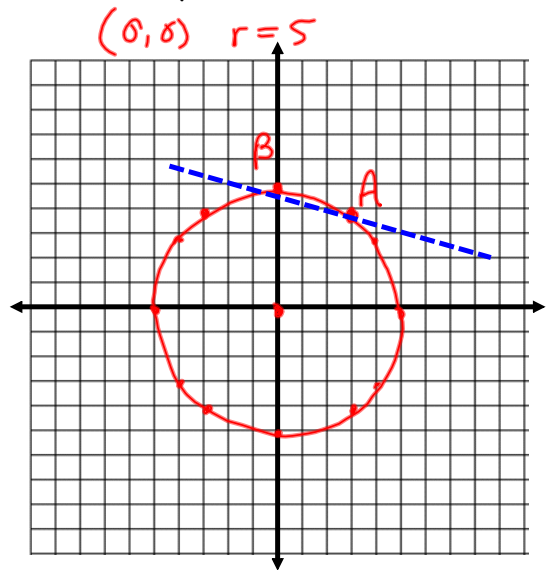
B(0,5)

$$y = mx + b$$

$$5 = -\frac{1}{3}(0) + b$$

$$5 = b$$

$$y = -\frac{1}{3}x + 5$$



Ex. 4: Find the coordinates of the points of intersection of the circle  $x^2 + y^2 = 100$  and the line  $x + y = 14$ . Is the line a secant or a tangent?

$$\begin{array}{r} x + y = 14 \\ -x \quad -x \\ \hline y = -x + 14 \end{array} \quad \begin{array}{l} x^2 + y^2 = 100 \\ \cdot \\ x^2 + (-x + 14)^2 = 100 \end{array}$$

$$x^2 + (-x + 14)(-x + 14) = 100$$

$$x^2 + x^2 - 14x - 14x + 196 = 100$$

$$\frac{2x^2 - 28x + 196}{-100 \quad -100} = 100$$

$$\frac{2x^2 - 28x + 96}{\frac{2}{2} \quad \frac{2}{2} \quad \frac{96}{2} \quad \frac{2}{2}} = 0$$

$$x^2 - 14x + 48 = 0$$

$$(x - 6)(x - 8) = 0 \rightarrow \text{find } y$$

$$x = 6, 8$$

$$\begin{array}{l} (6, 8) \\ x + y = 14 \\ 6 + y = 14 \\ y = 8 \end{array}$$

$$\begin{array}{l} (8, 6) \\ 8 + y = 14 \\ y = 6 \end{array}$$

